

Seasonal Photochemical and Meridional Transport Model for the Stratosphere of Titan

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A two-dimensional photochemical transport model is developed for Titan's stratosphere. Transformed Eulerian mean equations are used to determine the meridional circulation. Mechanical forcing is modeled using eddy and Rayleigh friction, while thermal forcing is provided by Newtonian and eddy heating. The model contains 117 photolysis, chemical, and condensation reactions for 22 hydrocarbon species along with atomic and molecular hydrogen. The method of conservation of second-order moments is used for the meridional and vertical advection calculations (Prather, M. J. 1986. *J. Geophys. Res.* 91, 6671–6681.).

Coustenis and Bézard (1995. *Icarus* 115, 126–140) analyzed the Voyager IRIS data to calculate hydrocarbon abundances from 53°S to 70°N. They determined that the ethane mixing ratio was approximately constant for all sampled latitudes. In the absence of meridional transport, photochemistry would yield higher concentrations of C₂ and C₃ hydrocarbon species near the equator than near the poles. Meridional advection results in enough tracer transport from low to high latitudes that the latitudinal distributions for ethane are much more uniform.

The model shows methane is well mixed in Titan's stratosphere. Model mixing ratios for ethane and propane agree well with Voyager IRIS data; however, the model overestimates the abundances of acetylene and diacetylene. The model abundance for methylacetylene is within the Voyager observational uncertainty, but the abundance for mid-southern latitudes is at the high end of this uncertainty. The model does not accurately reproduce the observed ethylene abundances.

Mid-latitude column densities (above 5 mbar) for ethane, propane, acetylene, and methylacetylene vary seasonal by 10, 14, 9.5, and 12%, respectively. Large seasonal variations for short-lived chemical species results in significant seasonal variations in the chemical production rates for organic polymers at middle and high latitudes.

Key Words: Titan; atmosphere, composition; photochemistry.

1. INTRODUCTION

The Voyager 1 spacecraft encountered Titan November 13, 1980, passing within 3500 km of the surface. The ultraviolet instrument detected the presence of nitrogen, leading to the conclusion that the atmosphere is predominantly molecular nitrogen (Broadfoot *et al.* 1981, Strobel and Shemansky 1982). The in-

frared instrument (IRIS) found strong emission features from CH₄, C₂H₂, C₂H₄, C₂H₆, and HCN (Hanel *et al.* 1981). Also identified in Titan's atmosphere were C₃H₈, CH₃CCH, C₄H₂, HC₃N, C₂N₂, and CO₂ (Kunde *et al.* 1981, Maguire *et al.* 1981, and Samuelson *et al.* 1983).

Visual imaging of Titan (Smith *et al.* 1981) did not reveal the surface but instead a global haze layer surrounding the satellite. Titan's northern hemisphere was found to be much darker and redder than the southern hemisphere. Southern mid-latitudes had albedos 25% greater than northern mid-latitudes. Also, in the northern hemisphere there was a dark polar hood above latitude 60°. The albedo of this dark polar region was approximately 7% less than northern mid-latitudes. No such feature was seen at the south pole. It was noted during the Voyager 1 encounter, which occurred near the northern hemisphere vernal equinox, that the albedo boundary between the hemispheres was at latitude 5°S, having moved south by 10° since the flyby of Pioneer 11 fourteen months earlier. This was opposite to the motion of the subsolar point and most likely an effect from Titan's 29.7 year seasonal cycle (Sromovsky *et al.* 1981). The hemispheric albedo asymmetry was reversed two seasons later as observed by the Hubble space telescope (Caldwell *et al.* 1992), confirming this seasonal effect.

A more complete analysis of the Voyager infrared data showed that latitudinal variations in brightness temperature existed in addition to the visual albedo variations. Spectra were taken for 200, 530, and 1304 cm⁻¹ over a 6-h period when the spacecraft was within 200,000 km of Titan. The field of view was a third of Titan's radius. The brightness temperature at 200 cm⁻¹ corresponds to roughly the tropopause temperature, with most of the opacity assumed to be due to CH₄ clouds just below the tropopause (Flasar *et al.* 1981). The northern hemisphere was found to be approximately 1 K warmer than the southern hemisphere at this wavenumber. The 530-cm⁻¹ spectra probe very close to the surface and the brightness temperature should be near the actual surface temperature. At 530 cm⁻¹ the spectra at low latitudes showed the northern hemisphere to be slightly warmer than the southern hemisphere, again by approximately 1 K, consistent with the tropopause temperature difference interpreted from the 200-cm⁻¹ spectra.

The situation is much different in the upper stratosphere, where the radiative response time is estimated to be on the order of 1 year (Flasar *et al.* 1981). This is much longer than the 16-day rotational period of Titan, implying that diurnal temperature variations should be minimal, but it is much shorter than the seasonal period, implying that meridional upper stratospheric temperatures should not lag significantly behind the seasonal forcing. Since the Voyager flyby occurred near the northern spring equinox, hemispherically symmetric brightness temperatures should have been seen. However, the brightness temperatures in the upper stratosphere (0.3 mbar level) were not symmetric between the two hemispheres (Flasar *et al.* 1981). A more recent work by Coustenis and Bézard (1995) estimates the temperature difference from the IRIS data between 50°N and 53°S latitude to be 7 K at 1 mbar pressure, the south being warmer.

As previously mentioned, the asymmetry in the hemispheric temperatures was accompanied by asymmetries in the visible albedo of the satellite. The southern hemisphere had a higher temperature and was visually brighter. It is not known whether these two phenomena originated at different levels in the atmosphere. The hemispheric differences in brightness may be caused by (1) differences in height or number density of atmospheric species, (2) variations in particle size or composition, or (3) dynamics coupled with one of the above (Smith *et al.* 1981). Hutzell *et al.* (1996) developed a 2-D model to study the effect of atmospheric motion of Titan's haze layer. They were unable to produce the latitudinal distribution of reflectivity seen during the Voyager 1 encounter. Flasar and Conrath (1990) have made a case for a dynamical explanation of the observed infrared emissions. However, they have not ruled out the possibility of an asymmetry in the meridional distribution of opacity. They suggest that it may be necessary to supplement their model and explain all of the Voyager observations. Bézard *et al.* (1995) calculated that latitudinal variations in gas and haze composition alone could account for the temperature asymmetry without the need to invoke dynamical inertia. Photochemical and transport modeling is needed to explain any of these seasonal variations in opacity.

Prior to the Voyager I encounter with Saturn, theoretical studies of Titan's atmosphere only involved hydrocarbon photochemistry (Strobel 1974, Caldwell 1978, Allen *et al.* 1980). A comprehensive post-Voyager one-dimensional (1-D) photochemical model was developed for the atmosphere of Titan by Yung *et al.* (1984). Yung *et al.* (1984) investigated the photochemistry of simple molecules containing carbon, hydrogen, nitrogen, and oxygen in the atmosphere of Titan. They incorporated the most up-to-date chemical schemes and reaction rate coefficients at that time. For rate coefficients that were unknown, they made estimates based on similar reactions. They started with an atmosphere that contained N₂, CH₄, and H₂O. The amount of N₂ was held constant, CH₄ was given a fixed mixing ratio (0.02) at the lower boundary, and a constant downward flux of H₂O was assumed at the upper boundary. They incorporated

24 photolysis reactions, 65 chemical reactions involving hydrocarbons only, and 35 chemical reactions involving nitrogen- and oxygen-containing species.

Yung *et al.* (1984) performed their calculations using a latitude of 30°, assuming this was representative of a global average, and incorporated eddy and molecular diffusion in the vertical direction. Their model set the lower boundary at the tropopause and the upper boundary at an altitude of 1160 km (except for H and H₂, where they used 1425 km for Jeans escape calculations). Their temperature profile was after Lindal *et al.* (1983) for the stratosphere, with an isothermal temperature profile for altitudes above the stratosphere. Setting diffusion boundary conditions for long-lived species at the tropopause and photochemical equilibrium for short-lived species, and only allowing H and H₂ to gravitationally escape, Yung *et al.* (1984) solved the continuity equation in spherical coordinates using a finite-difference iterative algorithm. They then compared their results to observational data from the Voyager studies.

The photochemical model of Yung *et al.* (1984) yielded a mixing ratio for CH₄ at the upper boundary, in excellent agreement with the results of the Voyager UVS experiment. Their values for the abundances of C₂H₆, H₂, HC₃N, and C₂N₂ were also consistent with the inferred Voyager analysis. For C₂H₄ the model was about a factor of 10 too low, while for C₂H₂ the model was a factor of 2 higher than Voyager IRIS observations. For C₄H₂ their model calculated abundance was 10–100 times lower than the observational estimates, while the CO calculated abundance was a factor of 3 higher than observed abundance.

More recent 1-D photochemical models were developed by Toubanc *et al.* (1995) and Lara *et al.* (1996). Both of these works had improvements over that by Yung *et al.* (1984) in that they used an updated CH₄ photodissociation scheme, an eddy diffusion coefficient profile constrained by more recent observational data, current values for chemical reaction rate coefficients, and a more rigorous treatment of the transfer of solar radiation. In addition, whereas Yung *et al.* assumed a CH₄ mixing ratio of 0.02 in the stratosphere, Toubanc *et al.* adopted a value of 0.016 and Lara *et al.* used a nominal value of 0.017.

Both of these recent models yielded a mole fraction for CH₄ at 1140 km of 10% compared to 8.3% from Yung *et al.* (1984) and 8 ± 3% from the Voyager UVS observations. Their results for C₂H₂ and C₂H₆ are much closer than Yung *et al.* to the inferred Voyager IRIS data for the lower stratosphere, but these two new models disagree by an order of magnitude on the ethane abundance in the upper stratosphere. Like Yung *et al.*, Toubanc *et al.* had difficulty matching the observed abundance for C₄H₂. Lara *et al.* had difficulty matching the observed abundances for both C₄H₂ and C₃H₈.

Although 1-D photochemical models are very useful for understanding the processes that are occurring in Titan's atmosphere, a two-dimensional (2-D) model is needed to increase our understanding of the observed seasonal variations. The purpose of this investigation is to develop a simple 2-D, zonally

averaged, photochemical transport model for the atmosphere of Titan and to use it to analyze latitudinal variations in hydrocarbon abundance in the stratosphere of Titan as the seasons progress.

2. TWO-DIMENSIONAL PHOTOCHEMICAL TRANSPORT MODELS

Two-dimensional photochemical transport models are inherently more complex than 1-D models. One-dimensional models typically incorporate local chemistry, photolysis, radiative transfer, and vertical eddy and molecular diffusion. These models use a specific latitude and season and assume diurnal and zonal averages. Two-dimensional photochemical transport models must also incorporate local chemistry, photolysis, radiative transfer, and eddy and molecular diffusion. In addition to these effects, a 2-D model must incorporate vertical and meridional transport of atmospheric species, as well as latitudinal variations in thermodynamic parameters, including seasonal insolation. Zonal averaging is usually assumed along surfaces that are constant with respect to the vertical coordinate.

To model tracer transport in a time-dependent 2-D photochemical model, the dynamical motion of the atmosphere must be calculated. This is usually done using a 2-D or 3-D general circulation model (GCM) that incorporates detailed solar heating and radiative cooling calculations. Many of these models, originally developed for the Earth's atmosphere, have been modified for studies of other planetary atmospheres. These GCM models, like the comprehensive 1-D photochemical models, are typically very computationally intensive by themselves. To date, no 2-D photochemical transport models have been developed for Titan. However, as this work will show, if appropriate approximations are made to reduce the computational complexity, a simple 2-D model can be used for a first-order study of the seasonal variation in hydrocarbon abundance in Titan's stratosphere.

All photochemical transport models must make use of the continuity equation as it applies to each atmospheric constituent. The continuity equation for the mixing ratio, μ_i , of the i th trace species is

$$\frac{\partial \mu_i}{\partial t} + \mathbf{v} \cdot \nabla \mu_i + \frac{1}{N} \nabla \cdot \phi_i = \frac{P_i}{N} - L_i \mu_i, \quad (1)$$

where

- t is time
- \mathbf{v} is velocity
- P_i is photochemical production rate of the i th species per unit volume
- L_i is photochemical loss rate of the i th species
- N is number density of the background atmosphere
- ϕ_i is diffusive flux of the i th species.

The continuity equations for the trace species are coupled with dynamical and thermodynamical equations for which no analyt-

ical solutions exist. As in 1-D models, 2-D models must make use of numerical methods to solve for the distribution of each atmospheric constituent.

A comprehensive 2-D photochemical model was developed for the stratosphere of Uranus by McMillan (1992). In this model, a numerical technique known as operator-splitting was employed to solve the coupled equations. Using operator-splitting, Eq. (1) is rewritten as

$$\frac{\partial \mu_i}{\partial t} = \left[\frac{\partial \mu_i}{\partial t} \right]_{\text{photochemistry}} + \left[\frac{\partial \mu_i}{\partial t} \right]_{\text{advection}} + \left[\frac{\partial \mu_i}{\partial t} \right]_{\text{diffusion}}, \quad (2)$$

where

$$\left[\frac{\partial \mu_i}{\partial t} \right]_{\text{photochemistry}} = \frac{P_i}{N} - L_i \mu_i. \quad (3)$$

$$\left[\frac{\partial \mu_i}{\partial t} \right]_{\text{advection}} = -\mathbf{v} \cdot \nabla \mu_i, \quad (4)$$

and

$$\left[\frac{\partial \mu_i}{\partial t} \right]_{\text{diffusion}} = -\frac{1}{N} \nabla \cdot \phi_i. \quad (5)$$

The photochemical-transport model presented in this paper uses the techniques of operator-splitting. First, the atmosphere is divided into a numerical grid. Photochemical reaction calculations are performed to determine the chemical production and loss rates for each grid cell for the current time step. Equation (3) is then solved. Next, a dynamical model is used to determine the meridional circulation. The resulting velocity field is used to calculate the advective mass transport and Eq. (4) is solved. Finally, eddy and molecular diffusion are accounted for by solving Eq. (5). The process is repeated for the next time step. The next three sections will discuss the numerical techniques used to solve Eqs. (3)–(5).

3. HYDROCARBON PHOTOCHEMISTRY

The treatment of photochemistry in a 2-D photochemical transport model is very similar to its treatment in a 1-D model. This is because chemical reactions are essentially local processes that depend on the physical conditions and molecular concentrations of each species in each grid cell. However, the number of photons available to interact with a species that can be photodissociated does depend on the total number of absorbing species along the optical path to each grid cell. So, indirectly, the production and/or loss of some chemical species is dependent on non-local conditions.

In 1-D photochemical models, the optical path is chosen to be either vertically downward or vertically downward with the

incorporation of a factor to account for a diurnally averaged solar zenith angle. A 2-D time-dependent model must account for the variation of zenith angle with the latitude and season, but the basic physics is the same as in 1-D models. Photodissociation processes are treated similarly to those in Summers and Strobel (1989). The rate of photodissociation of a species, i , is given by

$$J_i(z) = \int_{\lambda_1}^{\lambda_2} \sigma_{i,\lambda} \Phi(z, \lambda) d\lambda. \quad (6)$$

Here, λ is the wavelength, $\sigma_{i,\lambda}$ is the absorption cross section as a function of wavelength, and $\Phi(z, \lambda)$ is the solar flux at altitude z and wavelength λ . The flux $\Phi(z, \lambda)$ has dimensions of photons per unit area per second per wavelength. The wavelength region for photodissociation is 1000–2600 Å. We can express $\Phi(z, \lambda)$ as a function of the diurnally averaged unattenuated flux at the top of the atmosphere, $\Phi_\infty(\lambda)$,

$$\Phi(z, \lambda) = \Phi_\infty(\lambda) \exp \left\{ - \int_z^\infty \left[\sum_i \sigma_{i,\lambda} n_i(z') \right] \alpha_{z'} dz' \right\}. \quad (7)$$

In Eq. (7), n_i is the number density of the i th photoreactive species and α is the Chapman function of the solar zenith angle (Lara *et al.* 1996).

In numerical form the integral in Eq. (6) is replaced with a summation over wavelength bins 50 Å wide. The flux due to L_y - α is treated separately and added to the summation. Equation (6) becomes

$$J_i(z) = \sigma_{i,L_y-\alpha} F(z, \lambda_{L_y-\alpha}) + \sum_{w=1}^{32} \sigma_{i,\lambda_w} F(z, \lambda_w), \quad (8)$$

where $F(z, \lambda)$ is the solar flux at altitude z and wavelength λ in dimensions of photons per unit area per second. In Eq. (8), the integration is replaced with a summation over all the vertical grid cells. This yields

$$F(z, \lambda) = F_\infty(\lambda) \exp \left\{ - \sum_k \left[\sum_i \sigma_{i,\lambda} n_i(k) \right] \alpha \Delta z \right\}. \quad (9)$$

Not explicitly shown in Eqs. (8) and (9) are the dependencies of the photolysis rate on the latitude and season. The photolysis rate $J_i(z)$ is really $J_i(\phi, z, t)$, where ϕ is the latitude and t is time. Corrections to Eqs. (8) and (9) to account for the latitude and seasonal dependence are found in Cogley and Borucki (1976). This work has adopted Cogley and Borucki's approximation 4 to perform these calculations. The unattenuated solar flux at the top of the atmosphere and the attenuation of the solar flux due to Titan's aerosols are treated in the same manner as in Lara *et al.* (1996).

The 24 chemical species considered in this model are listed in Table I. This list contains all C₁–C₃ hydrocarbons, several C₄ hydrocarbons important in the formation of polymers, and molecular and atomic hydrogen. Table II lists the photolysis reactions while Tables III and IV contain the termolecular and

TABLE I
Chemical Species Used in the Photochemical Model

| Index | Formula | Name | Alternate name(s) |
|-------|----------------------------------|---------------------------|-----------------------|
| 1 | CH ₄ | methane | |
| 2 | C ₂ H ₆ | ethane | |
| 3 | C ₂ H ₂ | acetylene | ethyne |
| 4 | C ₃ H ₈ | propane | |
| 5 | CH ₃ CCH | methylacetylene | propyne, allylene |
| 6 | C ₂ H ₄ | ethylene | ethene |
| 7 | C ₄ H ₂ | diacetylene | 1,3-butadiyne |
| 8 | C ₃ H ₆ | propylene | propene |
| 9 | CH ₂ CCH ₂ | allene | propadiene |
| 10 | C ₃ H ₃ | allenyl | propynyl |
| 11 | CH ₃ | methyl | |
| 12 | ¹ CH ₂ | methylene (excited state) | |
| 13 | ³ CH ₂ | methylene (ground state) | |
| 14 | CH | methylidyne | |
| 15 | C ₂ H | ethynyl | |
| 16 | C ₂ H ₃ | vinyl | ethenyl |
| 17 | C ₂ H ₅ | ethyl | |
| 18 | C ₃ H ₂ | allenylcarbene | propynylidene |
| 19 | C ₃ H ₅ | allyl | propenyl, propylidene |
| 20 | C ₃ H ₇ | propyl | |
| 21 | C ₄ H | butadiynyl | |
| 22 | C ₄ H ₃ | butenylyl | butatrienyl |
| 23 | H | atomic hydrogen | |
| 24 | H ₂ | molecular hydrogen | |

bimolecular chemical reactions, respectively. Condensation processes are treated identically to those in Yung *et al.* (1984).

To solve for the abundance variations in each grid cell due to photochemistry, the time-dependent explicit finite difference form of Eq. (3) is employed:

$$\mu_i^n = \frac{P_i^{n-1} \Delta t}{N} + (1 - L_i^{n-1} \Delta t) \mu_i^{n-1}. \quad (10)$$

Solutions using Eq. (10) are accurate and stable for chemical species whose photochemical lifetimes are greater than the time step, Δt . For short-lived species, photochemical equilibrium is used to solve for the mixing ratios,

$$\mu_i^n = \frac{P_i^{n-1}}{L_i^{n-1} N}. \quad (11)$$

For the species that do not clearly fall into either the long-lived or the short-lived group, Eq. (10) is used to solve for their mixing ratios for grid cells in which their photochemical lifetimes exceed Δt . Equation (11) is used to solve for their mixing ratios for grid cells in which their photochemical lifetimes are less than Δt .

4. DYNAMICAL MODEL FOR TITAN'S STRATOSPHERE

For Titan, the Coriolis parameter is sufficiently small, due to its slow rotational rate, that cyclostrophic terms cannot be

TABLE II
Photodissociation Reactions for Titan Model Atmosphere

| Index | Reactions | Quantum yield | | Reference |
|-------|---|---------------|-------|------------------------------|
| | | Ly- α | Other | |
| P11 | $\text{CH}_4 + h\nu \rightarrow {}^1\text{CH}_2 + \text{H}_2$ | 0.22 | 0 | Heck <i>et al.</i> 1996 |
| P12 | $\text{CH}_4 + h\nu \rightarrow \text{CH}_3 + \text{H}$ | 0.67 | 1 | Heck <i>et al.</i> 1996 |
| P13 | $\text{CH}_4 + h\nu \rightarrow \text{CH} + \text{H} + \text{H}_2$ | 0.11 | 0 | Heck <i>et al.</i> 1996 |
| P21 | $\text{C}_2\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H}_4 + \text{H}_2$ | 0.12 | 0.56 | Akimoto <i>et al.</i> 1965 |
| P22 | $\text{C}_2\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H}_4 + 2\text{H}$ | 0.3 | 0.14 | Hampson <i>et al.</i> 1965 |
| P23 | $\text{C}_2\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H}_2 + 2\text{H}_2$ | 0.25 | 0.27 | Lias <i>et al.</i> 1970 |
| P24 | $\text{C}_2\text{H}_6 + h\nu \rightarrow \text{CH}_4 + {}^1\text{CH}_2$ | 0.25 | 0.02 | Mount <i>et al.</i> 1978 |
| P25 | $\text{C}_2\text{H}_6 + h\nu \rightarrow 2\text{CH}_3$ | 0.08 | 0.01 | Mount <i>et al.</i> 1978 |
| P31 | $\text{C}_2\text{H}_2 + h\nu \rightarrow \text{C}_2\text{H} + \text{H}$ | 0.3 | 0.06 | Nakayawa <i>et al.</i> 1964 |
| P32 | $\text{C}_2\text{H}_2 + h\nu \rightarrow \text{C}_2 + \text{H}_2$ | 0.1 | 0.1 | Okabe 1981, 1983 |
| P41 | $\text{C}_3\text{H}_8 + h\nu \rightarrow \text{C}_3\text{H}_6 + \text{H}_2$ | 0.33 | 0.94 | Calvert and Pitts 1966 |
| P42 | $\text{C}_3\text{H}_8 + h\nu \rightarrow \text{C}_2\text{H}_6 + {}^1\text{CH}_2$ | 0.09 | 0 | Calvert and Pitts 1966 |
| P43 | $\text{C}_3\text{H}_8 + h\nu \rightarrow \text{C}_2\text{H}_5 + \text{CH}_3$ | 0.38 | 0 | Calvert and Pitts 1966 |
| P44 | $\text{C}_3\text{H}_8 + h\nu \rightarrow \text{C}_2\text{H}_4 + \text{CH}_4$ | 0.2 | 0.06 | Calvert and Pitts 1966 |
| P51 | $\text{CH}_3\text{CCH} + h\nu \rightarrow \text{C}_3\text{H}_3 + \text{H}$ | 0.4 | 0.4 | Stief <i>et al.</i> 1971 |
| P52 | $\text{CH}_3\text{CCH} + h\nu \rightarrow \text{C}_3\text{H}_2 + \text{H}_2$ | 0.15 | 0.15 | Hamai <i>et al.</i> 1979 |
| P53 | $\text{CH}_3\text{CCH} + h\nu \rightarrow \text{CH}_3 + \text{C}_2\text{H}$ | 0.2 | 0.2 | Hamai <i>et al.</i> 1979 |
| P61 | $\text{C}_2\text{H}_4 + h\nu \rightarrow \text{C}_2\text{H}_2 + \text{H}_2$ | 0.51 | 0.51 | Zelikoff <i>et al.</i> 1953 |
| P62 | $\text{C}_2\text{H}_4 + h\nu \rightarrow \text{C}_2\text{H}_2 + 2\text{H}$ | 0.49 | 0.49 | Back <i>et al.</i> 1967 |
| P71 | $\text{C}_4\text{H}_2 + h\nu \rightarrow \text{C}_4\text{H} + \text{H}$ | 0.2 | 0.03 | Summers <i>et al.</i> 1989 |
| P72 | $\text{C}_4\text{H}_2 + h\nu \rightarrow 2\text{C}_2\text{H}$ | 0.03 | 0.01 | Summers <i>et al.</i> 1989 |
| P73 | $\text{C}_4\text{H}_2 + h\nu \rightarrow \text{C}_2\text{H}_2 + \text{C}_2$ | 0.1 | 0.02 | Summers <i>et al.</i> 1989 |
| P74 | $\text{C}_4\text{H}_2 + h\nu \rightarrow \text{C}_4\text{H}_2^{**}$ | 0.67 | 0.67 | Summers <i>et al.</i> 1989 |
| P81 | $\text{C}_3\text{H}_6 + h\nu \rightarrow \text{CH}_2\text{CCH}_2 + \text{H}_2$ | 0.57 | 0.57 | Calvert and Pitts 1966 |
| P82 | $\text{C}_3\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H}_4 + \text{CH}_2$ | 0.02 | 0.02 | Borrell <i>et al.</i> 1971 |
| P83 | $\text{C}_3\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H}_2 + \text{CH}_3 + \text{H}$ | 0.34 | 0.34 | Collin <i>et al.</i> 1979 |
| P84 | $\text{C}_3\text{H}_6 + h\nu \rightarrow \text{C}_2\text{H} + \text{CH}_4 + \text{H}$ | 0.05 | 0.05 | Collin 1973 |
| P91 | $\text{CH}_2\text{CCH}_2 + h\nu \rightarrow \text{C}_3\text{H}_3 + \text{H}$ | 0.4 | 0.4 | Sutcliffe <i>et al.</i> 1952 |
| P92 | $\text{CH}_2\text{CCH}_2 + h\nu \rightarrow \text{C}_3\text{H}_2 + \text{H}_2$ | 0.15 | 0.15 | Rabelais <i>et al.</i> 1971 |
| P93 | $\text{CH}_2\text{CCH}_2 + h\nu \rightarrow \text{C}_2\text{H}_2 + \text{CH}_2$ | 0.06 | 0.06 | Heller and Milne 1978 |
| P10 | $\text{C}_3\text{H}_3 + h\nu \rightarrow \text{C}_3\text{H}_2 + \text{H}$ | 1 | 1 | Jacox <i>et al.</i> 1974 |

neglected in dynamical equations. The transformed Eulerian-mean (TEM) equations (Andrews *et al.* 1987) are used for the meridional circulation in Titan's stratosphere since they are easily solved in the cyclostrophic regime. The meridional and vertical velocities used in the TEM equations are good approximations for advective transport calculations (Andrews *et al.* 1987).

In spherical log pressure coordinates the TEM primitive set of equations is

$$\frac{\partial \bar{u}}{\partial t} + \bar{v}^* \left[\frac{1}{a \cos \phi} \frac{\partial (\bar{u} \cos \phi)}{\partial \phi} - f \right] + \bar{w}^* \frac{\partial \bar{u}}{\partial z} - \bar{X} = \frac{1}{\rho_0 r \cos \phi} \nabla \cdot \mathbf{F} \quad (12)$$

$$\bar{u} \left[f + \frac{\bar{u} \tan \phi}{a} \right] + \frac{1}{a} \frac{\partial \bar{\Phi}}{\partial \phi} = G \quad (13)$$

$$\frac{\partial \bar{\Phi}}{\partial z} - \frac{R}{H_0} \bar{\theta} \exp\left(-\frac{\kappa z}{H_0}\right) = 0 \quad (14)$$

$$\frac{1}{a \cos \phi} \frac{\partial}{\partial \phi} (\bar{v}^* \cos \phi) + \frac{1}{\rho_0} \frac{\partial}{\partial z} (\rho_0 \bar{w}^*) = 0 \quad (15)$$

$$\begin{aligned} \frac{\partial \bar{\theta}}{\partial t} + \frac{\bar{v}^*}{a} \frac{\partial \bar{\theta}}{\partial \phi} + \bar{w}^* \frac{\partial \bar{\theta}}{\partial z} - \bar{Q} \\ = -\frac{1}{\rho_0} \left[\frac{1}{a} \frac{\partial}{\partial z} \left(\rho_0 \frac{\overline{v'\theta'}}{(\partial \bar{\theta} / \partial z)} \frac{\partial \bar{\theta}}{\partial \phi} \right) + \frac{\partial}{\partial z} (\rho_0 \overline{w'\theta'}) \right]. \end{aligned} \quad (16)$$

Equations (12) and (13) are the zonal and meridional momentum balances, respectively. Equation (14) is called the hydrostatic equation, Eq. (15) is the continuity equation, and Eq. (16) is the heat equation. The symbols for these equations are defined in Table V. The bars denote zonal averages, the primes denote deviations from the zonal averages, and the asterisks denote residual velocities (Andrews *et al.* 1987).

TABLE III
Termolecular Chemical Reactions

| Reaction | Rate coefficients ^a | Reference |
|---|--|------------------------------|
| 1 H + H + M → H ₂ + M | $k_0 = 2.5 \times 10^{-31} T^{-0.6}$ $k_\infty = 1.0 \times 10^{-11}$ | Baulch <i>et al.</i> 1992 |
| 2 CH + H ₂ + M → CH ₃ + M | $k_0 = 3.8 \times 10^{-29} e^{-20/T}$ $k_\infty = 2.4 \times 10^{-12} e^{523/T}$ | Gladstone <i>et al.</i> 1996 |
| 3 ³ CH ₂ + H + M → CH ₃ + M | $k_0 = 3.1 \times 10^{-30} e^{-457/T}$ $k_\infty = 1.5 \times 10^{-11}$ | Summers and Strobel 1989 |
| 4 C ₃ H ₇ + H + M → C ₃ H ₈ + M | $k_0 = 1.0 \times 10^{-22} e^{341/T}$ $k_\infty = 1.7 \times 10^{-10}$ | Gladstone <i>et al.</i> 1996 |
| 5 C ₂ H ₃ + C ₂ H ₃ + M → C ₄ H ₆ + M | $k_0 = 8.76 \times 10^{-6} e^{-1390/T} T^{-7.0}$ $k_\infty = 8.2 \times 10^{-11}$ | Gladstone <i>et al.</i> 1996 |
| 6 CH ₃ + H + M → CH ₄ + M | $k_0 = 3.8 \times 10^{-28} e^{-20/T}$ $k_\infty = 2.1 \times 10^{-10}$ | Gladstone <i>et al.</i> 1996 |
| 7 2CH ₃ + M → C ₂ H ₆ + M | $k_0 = 8.76 \times 10^{-7} e^{-1390/T} T^{-7.0}$ $k_\infty = 1.4 \times 10^{-9} e^{-329/T}$ | Gladstone <i>et al.</i> 1996 |
| 8 CH ₃ + C ₂ H ₃ + M → C ₃ H ₆ + M | $k_0 = 1.3 \times 10^{-22}$ $k_\infty = 9.1 \times 10^{-12}$ | Yung <i>et al.</i> 1984 |
| 9 CH ₃ + C ₂ H ₅ + M → C ₃ H ₈ + M | $k_0 = 1.0 \times 10^{-22} e^{341/T}$ $k_\infty = 8.1 \times 10^{-11}$ | Gladstone <i>et al.</i> 1996 |
| 10 C ₂ H + H + M → C ₂ H ₂ + M | $k_0 = 1.3 \times 10^{-18} e^{-721/T} T^{-3.1}$ $k_\infty = 3.0 \times 10^{-10}$ | Tsang <i>et al.</i> 1986 |
| 11 C ₂ H ₂ + H + M → C ₂ H ₃ + M | $k_0 = 6.4 \times 10^{-25} e^{-1200/T} T^{-2.0}$ $k_\infty = 3.8 \times 10^{-11} e^{-1374/T}$ | Gladstone <i>et al.</i> 1996 |
| 12 C ₂ H ₄ + H + M → C ₂ H ₅ + M | $k_0 = 2.15 \times 10^{-29} e^{-349/T}$ $k_\infty = 4.4 \times 10^{-11} e^{-1087/T}$ | Gladstone <i>et al.</i> 1996 |
| 13 2C ₂ H ₅ + M → C ₄ H ₁₀ + M | $k_0 = 1.55 \times 10^{-22} e^{586/T}$ $k_\infty = 1.4 \times 10^{-11} e^{35.2/T}$ | Gladstone <i>et al.</i> 1996 |
| 14 C ₃ H ₂ + H + M → C ₃ H ₃ + M | $k_0 = 6.33 \times 10^{-29} e^{-20/T}$ $k_\infty = 3.0 \times 10^{-10}$ | Toublanc <i>et al.</i> 1995 |
| 15 C ₃ H ₃ + H + M → CH ₃ CCH + M | $k_0 = 6.33 \times 10^{-29} e^{-20/T}$ $k_\infty = 3.0 \times 10^{-10}$ | Toublanc <i>et al.</i> 1995 |
| 16 C ₃ H ₃ + H + M → CH ₂ CCH ₂ + M | $k_0 = 6.33 \times 10^{-29} e^{-20/T}$ $k_\infty = 3.0 \times 10^{-10}$ | Toublanc <i>et al.</i> 1995 |
| 17 CH ₂ CCH ₂ + H + M → CH ₃ + C ₂ H ₂ + M | $k_0 = 8.0 \times 10^{-24} e^{-1225/T} T^{-2.0}$ $k_\infty = 9.7 \times 10^{-12} e^{-1550/T}$ | Toublanc <i>et al.</i> 1995 |
| 18 CH ₂ CCH ₂ + H + M → C ₃ H ₅ + M | $k_0 = 8.0 \times 10^{-24} e^{-1225/T} T^{-2.0}$ $k_\infty = 1.4 \times 10^{-11} e^{-1000/T}$ | Toublanc <i>et al.</i> 1995 |
| 19 CH ₃ CCH + H + M → CH ₃ + C ₂ H ₂ + M | $k_0 = 8.0 \times 10^{-24} e^{-1225/T} T^{-2.0}$ $k_\infty = 9.7 \times 10^{-12} e^{-1550/T}$ | Toublanc <i>et al.</i> 1995 |
| 20 CH ₃ CCH + H + M → C ₃ H ₆ + M | $k_0 = 8.0 \times 10^{-24} e^{-1225/T} T^{-2.0}$ $k_\infty = 9.7 \times 10^{-12} e^{-1550/T}$ | Toublanc <i>et al.</i> 1995 |
| 21 C ₃ H ₅ + H + M → C ₃ H ₆ + M | $k_0 = 1.0 \times 10^{-28}$ $k_\infty = 1.7 \times 10^{-10}$ | Gladstone <i>et al.</i> 1996 |
| 22 C ₃ H ₆ + H + M → C ₃ H ₇ + M | $k_0 = 2.15 \times 10^{-28} e^{-349/T}$ $k_\infty = 2.6 \times 10^{-11} e^{-798/T}$ | Gladstone <i>et al.</i> 1996 |
| 23 C ₄ H + H + M → C ₄ H ₂ + M | $k_0 = 4.2 \times 10^{-19} e^{-721/T} T^{-3.1}$ $k_\infty = 1.0 \times 10^{-10}$ | Toublanc <i>et al.</i> 1995 |
| 24 C ₄ H ₂ + H + M → C ₄ H ₃ + M | $k_0 = 4.7 \times 10^{-21} e^{-1184/T} T^{-2.0}$ $k_\infty = 1.4 \times 10^{-10} e^{-1184/T}$ | Summers and Strobel 1989 |
| 25 C ₄ H ₃ + H + M → C ₄ H ₄ + M | $k_0 = 4.7 \times 10^{-21} e^{-1184/T} T^{-2.0}$ $k_\infty = 1.4 \times 10^{-10} e^{-1184/T}$ | Summers and Strobel 1989 |
| 26 C ₃ H ₇ + CH ₃ + M → C ₄ H ₁₀ + M | $k_0 = 2.5 \times 10^{-19}$ $k_\infty = 4.2 \times 10^{-11} e^{-200/T}$ | Yung <i>et al.</i> 1984 |

^a Units: k_0 , (cm⁶/s); k_∞ , (cm³/s).

TABLE IV
Bimolecular Chemical Reactions

| Reaction | Rate coefficient (cm ³ /s) | Reference |
|--|---|------------------------------|
| 1 CH + CH ₄ → C ₂ H ₄ + H | 5.0 × 10 ⁻¹¹ e ^{200/T} | Toublanc <i>et al.</i> 1995 |
| 2 CH + C ₂ H ₂ → C ₃ H ₂ + H | 3.49 × 10 ⁻¹⁰ e ^{61/T} | Gladstone <i>et al.</i> 1996 |
| 3 CH + C ₂ H ₄ → CH ₂ CCH ₂ + H | 2.23 × 10 ⁻¹⁰ e ^{173/T} | Gladstone <i>et al.</i> 1996 |
| 4 CH + C ₂ H ₆ → C ₃ H ₆ + H | 1.8 × 10 ⁻¹⁰ e ^{132/T} | Gladstone <i>et al.</i> 1996 |
| 5 ¹ CH ₂ + H ₂ → ³ CH ₂ + H ₂ | 1.26 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 6 ¹ CH ₂ + H ₂ → CH ₃ + H | 9.2 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 7 ¹ CH ₂ + CH ₄ → ³ CH ₂ + CH ₄ | 1.2 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 8 ¹ CH ₂ + CH ₄ → 2CH ₃ | 5.9 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 9 ¹ CH ₂ + N ₂ → ³ CH ₂ + N ₂ | 7.9 × 10 ⁻¹² | Yung <i>et al.</i> 1984 |
| 10 ³ CH ₂ + H → CH + H ₂ | 4.7 × 10 ⁻¹⁰ e ^{-370/T} | Gladstone <i>et al.</i> 1996 |
| 11 ³ CH ₂ + CH ₃ → C ₂ H ₄ + H | 7.0 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 12 ³ CH ₂ + ³ CH ₂ → C ₂ H ₂ + 2H | 2.1 × 10 ⁻¹⁰ e ^{-408/T} | Gladstone <i>et al.</i> 1996 |
| 13 ³ CH ₂ + C ₂ H ₅ → C ₂ H ₄ + CH ₃ | 3.0 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 14 CH ₃ + C ₂ H ₃ → C ₂ H ₂ + CH ₄ | 3.4 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 15 CH ₃ + C ₂ H ₅ → C ₂ H ₄ + CH ₄ | 4.7 × 10 ⁻¹² | Gladstone <i>et al.</i> 1996 |
| 16 C ₂ + CH ₄ → C ₂ H + CH ₃ | 5.1 × 10 ⁻¹¹ e ^{-297/T} | Gladstone <i>et al.</i> 1996 |
| 17 C ₂ + H ₂ → C ₂ H + H | 1.77 × 10 ⁻¹⁰ e ^{-1469/T} | Gladstone <i>et al.</i> 1996 |
| 18 C ₂ H + CH ₄ → C ₂ H ₂ + CH ₃ | 9.0 × 10 ⁻¹² e ^{-250/T} | Gladstone <i>et al.</i> 1996 |
| 19 C ₂ H + C ₂ H ₂ → C ₄ H ₂ + H | 1.5 × 10 ⁻¹⁰ | Gladstone <i>et al.</i> 1996 |
| 20 C ₂ H + C ₂ H ₄ → C ₄ H ₄ + H | 2.5 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 21 C ₂ H + C ₂ H ₆ → C ₂ H ₂ + C ₂ H ₅ | 3.62 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 22 C ₂ H + C ₃ H ₈ → C ₂ H ₂ + C ₃ H ₇ | 6.0 × 10 ⁻¹² | Toublanc <i>et al.</i> 1995 |
| 23 C ₂ H + C ₄ H ₂ → C ₆ H ₂ + H | 4.15 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 24 C ₂ H ₃ + H → C ₂ H ₂ + H ₂ | 6.0 × 10 ⁻¹² | Gladstone <i>et al.</i> 1996 |
| 25 C ₂ H ₃ + C ₂ H ₃ → C ₂ H ₄ + C ₂ H ₂ | 2.4 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 26 C ₂ H ₃ + C ₂ H ₅ → C ₂ H ₆ + C ₂ H ₂ | 8.0 × 10 ⁻¹³ | Gladstone <i>et al.</i> 1996 |
| 27 C ₂ H ₃ + C ₂ H ₅ → 2C ₂ H ₄ | 8.0 × 10 ⁻¹³ | Gladstone <i>et al.</i> 1996 |
| 28 C ₂ H ₅ + H → 2CH ₃ | 8.0 × 10 ⁻¹¹ e ^{-127/T} | Gladstone <i>et al.</i> 1996 |
| 29 C ₂ H ₅ + H → C ₂ H ₄ + H ₂ | 3.0 × 10 ⁻¹² | Gladstone <i>et al.</i> 1996 |
| 30 C ₂ H ₅ + C ₂ H ₅ → C ₂ H ₆ + C ₂ H ₄ | 1.2 × 10 ⁻¹¹ e ^{-540/T} | Gladstone <i>et al.</i> 1996 |
| 31 C ₃ H ₅ + H → C ₂ H ₂ + CH ₄ | 3.3 × 10 ⁻¹⁰ | Toublanc <i>et al.</i> 1995 |
| 32 C ₃ H ₅ + H → CH ₃ CCH + H ₂ | 3.3 × 10 ⁻¹⁰ | Toublanc <i>et al.</i> 1995 |
| 33 C ₃ H ₅ + H → CH ₂ CCH ₂ + H ₂ | 3.0 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 34 C ₃ H ₅ + CH ₃ → CH ₃ CCH + CH ₄ | 1.15 × 10 ⁻¹² e ^{66/T} | Toublanc <i>et al.</i> 1995 |
| 35 C ₃ H ₅ + CH ₃ → CH ₂ CCH ₂ + CH ₄ | 1.15 × 10 ⁻¹² e ^{66/T} | Toublanc <i>et al.</i> 1995 |
| 36 C ₃ H ₇ + H → C ₃ H ₆ + H ₂ | 5.0 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 37 C ₃ H ₇ + H → C ₂ H ₅ + CH ₃ | 6.0 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 38 C ₃ H ₇ + CH ₃ → C ₃ H ₆ + CH ₄ | 1.85 × 10 ⁻¹² e ^{339/T} | Toublanc <i>et al.</i> 1995 |
| 39 C ₄ H + CH ₄ → C ₄ H ₂ + CH ₃ | 9.3 × 10 ⁻¹³ e ^{-250/T} | Yung <i>et al.</i> 1984 |
| 40 C ₄ H + C ₂ H ₂ → C ₆ H ₂ + H | 1.0 × 10 ⁻¹¹ | Yung <i>et al.</i> 1984 |
| 41 C ₄ H + C ₂ H ₄ → C ₄ H ₂ + C ₂ H ₃ | 1.2 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 42 C ₄ H + C ₂ H ₆ → C ₄ H ₂ + C ₂ H ₅ | 2.1 × 10 ⁻¹¹ | Gladstone <i>et al.</i> 1996 |
| 43 C ₄ H + C ₄ H ₂ → C ₈ H ₂ + H | 5.81 × 10 ⁻¹¹ | Toublanc <i>et al.</i> 1995 |
| 44 C ₄ H ₂ ** + N ₂ → C ₄ H ₂ + N ₂ | 1.0 × 10 ⁻¹¹ | Summers and Strobel 1989 |
| 45 C ₄ H ₂ ** + C ₂ H ₂ → C ₆ H ₂ + H ₂ | 1.0 × 10 ⁻¹¹ | Summers and Strobel 1989 |
| 46 C ₄ H ₂ ** + C ₄ H ₂ → C ₈ H ₂ + H ₂ | 1.0 × 10 ⁻¹¹ | Summers and Strobel 1989 |
| 47 C ₄ H ₃ + H → 2C ₂ H ₂ | 3.3 × 10 ⁻¹² | Gladstone <i>et al.</i> 1996 |
| 48 C ₄ H ₃ + H → C ₄ H ₂ + H ₂ | 1.2 × 10 ⁻¹¹ | Yung <i>et al.</i> 1984 |
| 49 CH ₂ CCH ₂ + H → CH ₃ CCH + H | 1.0 × 10 ⁻¹¹ e ^{-1000/T} | Gladstone <i>et al.</i> 1996 |

The five primitive equations are used to derive the partial differential equation for the meridional circulation, where

$$\begin{aligned}
 & -\frac{2 \tan \phi}{a} \left(\hat{f} \bar{v}^* - \frac{\partial \bar{u}}{\partial z} \bar{w}^* \right) \frac{\partial \bar{u}}{\partial z} - \bar{f} \frac{\partial}{\partial z} (\hat{f} \bar{v}^*) + \bar{f} \frac{\partial}{\partial z} \left(\bar{w}^* \frac{\partial \bar{u}}{\partial y} \right) \\
 & + R^* \frac{\partial}{\partial y} \left(\bar{v}^* \frac{\partial \bar{\theta}}{\partial y} \right) + R^* \frac{\partial}{\partial y} (\hat{S} \bar{w}^*) = F_1, \quad (17)
 \end{aligned}$$

$$\hat{f} \equiv f - \frac{1}{a \cos \phi} \frac{\partial}{\partial \phi} (\bar{u} \cos \phi), \quad (18)$$

$$\bar{f} \equiv f + \frac{2 \tan \phi}{a} \bar{u}, \quad (19)$$

$$R^* \equiv \frac{R}{H_0} \exp \left(-\frac{\kappa z}{H_0} \right), \quad (20)$$

TABLE V
Parameters and Variables Used in the Dynamics Equations

| | |
|----------|--|
| a | equatorial radius of Titan's tropopause |
| z | log pressure altitude $\equiv -H_0 \ln(P/P_0)$ |
| ϕ | latitude |
| H_0 | reference scale height $\equiv 30$ km |
| R | gas constant |
| k | Boltzmann's constant |
| P | pressure |
| P_0 | reference pressure, tropopause pressure ≈ 144 mb |
| ρ_0 | horizontally averaged density $\equiv \rho_s \exp(-z/H_0)$, $\rho_s \equiv$ reference density |
| u | zonal velocity, positive in the direction of rotation |
| v | meridional velocity, positive toward the north |
| w | vertical velocity, positive up |
| Φ | geopotential |
| C_p | specific heat at constant pressure |
| κ | ratio of gas constant to specific heat, $\equiv R/C_p$ |
| T | temperature |
| θ | potential temperature |
| Ω | rotation rate of Titan |
| f | Coriolis parameter |
| Q | heating rate |
| G | zonally averaged eddy flux of heat term |
| τ_r | radiative time constant |
| τ_f | Rayleigh friction time constant |
| X | non-conservative force component in the zonal direction, F_{fr_x} |
| Y | non-conservative force component in meridional direction, F_{fr_y} |
| ψ | streamfunction |
| F | Eliassen-Palm flux |

and the static stability, \hat{S} , is used to approximate the vertical derivative of the mean potential temperature,

$$\hat{S} \approx \frac{\partial \bar{\theta}}{\partial z}. \quad (21)$$

The forcing term on the right-hand side of Eq. (17) is expressed in terms of mechanical forcing, M , and thermal forcing J as given by

$$F_1 = \tilde{f} \frac{\partial M}{\partial z} + \frac{2 \tan \phi}{a} M \frac{\partial \bar{u}}{\partial z} + R^* \frac{\partial J}{\partial y}, \quad (22)$$

where

$$M \equiv \frac{1}{\rho_0 a \cos \phi} \nabla \cdot \mathbf{F} + \bar{X}, \quad (23)$$

and

$$J \equiv \bar{Q} - \frac{1}{\rho_0} \left[\frac{1}{a} \frac{\partial}{\partial z} \left(\rho_0 \frac{\overline{v'\theta'}}{(\partial \bar{\theta}/\partial z)} \frac{\partial \bar{\theta}}{\partial \phi} \right) + \frac{\partial}{\partial z} (\rho_0 \overline{w'\theta'}) \right]. \quad (24)$$

Let

$$\bar{v}^* \equiv -\frac{1}{\cos \phi} \left(\frac{\partial \psi}{\partial z} - \frac{\psi}{H_0} \right) \quad \text{and} \quad \bar{w}^* \equiv \frac{1}{\cos \phi} \frac{\partial \psi}{\partial y} \quad (25a,b)$$

define the streamfunction. Equation (17) can now be written as

$$C_{11} \frac{\partial^2 \psi}{\partial y^2} + C_{12} \frac{\partial^2 \psi}{\partial y \partial z} + C_{22} \frac{\partial^2 \psi}{\partial z^2} + C_1 \frac{\partial \psi}{\partial y} + C_2 \frac{\partial \psi}{\partial z} + C_0 \psi = F, \quad (26)$$

where

$$C_{11} \equiv R^* \hat{S}, \quad C_{12} \equiv \tilde{f} \frac{\partial \bar{u}}{\partial z} - R^* \frac{\partial \bar{\theta}}{\partial y}, \quad C_{22} \equiv \tilde{f} \tilde{f} \quad (27a,b,c)$$

$$C_1 \equiv \tilde{f} \frac{\partial^2 \bar{u}}{\partial z^2} + R^* \left(\frac{\partial^2 \bar{\theta}}{\partial y \partial z} + \frac{1}{H_0} \frac{\partial \bar{\theta}}{\partial y} \right) + \frac{\tan \phi}{a} \left[2 \left(\frac{\partial \bar{u}}{\partial z} \right)^2 + R^* \hat{S} \right] \quad (28)$$

$$C_2 \equiv \frac{\partial \bar{u}}{\partial z} \left[\frac{\partial \tilde{f}}{\partial y} + \frac{2 \tan \phi}{a} (\hat{f} + \tilde{f}) \right] - \frac{\tilde{f} \tilde{f}}{H_0} \quad (29)$$

$$C_0 \equiv -\frac{1}{H_0} \frac{\partial \bar{u}}{\partial z} \left[\frac{\partial \tilde{f}}{\partial y} + \frac{2 \tan \phi}{a} (\hat{f} + \tilde{f}) \right] \quad (30)$$

and

$$F \equiv F_1 \cos \phi. \quad (32)$$

On a numerical grid, Eq. (26) is solved using a 7-point finite difference scheme. The finite difference form of Eq. (26) is

$$A_x \psi_{J+1,K} + C_x \psi_{J-1,K} + A_y \psi_{J,K+1} + C_y \psi_{J,K-1} + B_0 \psi_{J,K} + A_z \psi_{J-1,K-1} + C_z \psi_{J+1,K+1} = F_{J,K}. \quad (33)$$

where $\Delta y \equiv a \Delta \phi$. The array coefficients are defined by

$$\begin{aligned} A_x &= \left(\frac{C_{11}}{\Delta y^2} - \frac{C_{12}}{2 \Delta y \Delta z} + \frac{C_1}{2 \Delta y} \right) \\ A_y &= \left(-\frac{C_{12}}{2 \Delta y \Delta z} + \frac{C_{22}}{\Delta z^2} + \frac{C_2}{2 \Delta z} \right) \\ C_x &= \left(\frac{C_{11}}{\Delta y^2} - \frac{C_{12}}{2 \Delta y \Delta z} - \frac{C_1}{2 \Delta y} \right) \\ C_y &= \left(-\frac{C_{12}}{2 \Delta y \Delta z} + \frac{C_{22}}{\Delta z^2} - \frac{C_2}{2 \Delta z} \right) \\ B_0 &= \left(-\frac{2C_{11}}{\Delta y^2} - \frac{2C_{22}}{\Delta z^2} + \frac{C_{12}}{\Delta y \Delta z} + C_0 \right) \\ A_z &= C_z = \left(\frac{C_{12}}{2 \Delta y \Delta z} \right). \end{aligned} \quad (34)$$

Equation (33) is solved using the Gauss-Siedel method (Press *et al.* 1989). The boundary conditions assume zero meridional velocities at each pole and zero vertical velocities at the upper and lower boundaries, similar to Hutzell *et al.* (1996). The para

meters $A_x, A_y, A_z, C_x, C_y, C_z, B_0$, and $F_{J,K}$ are evaluated at all points (J, K) for each time step.

For simplicity in this model, the mechanical forcing will only be expressed in terms of eddy and Rayleigh friction. These forces are parameterized using

$$M = \frac{1}{\rho} \frac{\partial}{\partial z} \left(\rho K_{zz} \frac{\partial \bar{u}}{\partial z} \right) - \frac{\bar{u}}{\tau_f}. \quad (35)$$

Here K_{zz} is the eddy diffusion coefficient and τ_f the Rayleigh frictional damping time constant. Both K_{zz} and τ_f are free parameters in this model. Typically, in 1-D photochemical transport models, K_{zz} is adjusted until the results match the steady-state number density of a particular species whose abundance is well known. This work borrows the results from 1-D models to constrain the values for K_{zz} .

For computational simplicity, Newtonian cooling is used to model the net heating rate,

$$Q = \alpha_r (\bar{\theta} - \langle \bar{\theta} \rangle) = \frac{\bar{\theta} - \langle \bar{\theta} \rangle}{\tau_r}. \quad (36)$$

Here, α_r is the Newtonian cooling coefficient, equal to the reciprocal of the radiative time constant, τ_r . The brackets in Eq. (36) imply a meridional mean. Frictional damping constants for the stratospheres of planets are typically within an order of magnitude of the radiative time constants (McMillan 1992). Therefore, in this model the approximation $\tau_f = \tau_r$ is employed.

The eddy terms from Eq. (24) can be expressed using mixing length theory,

$$\begin{aligned} & \frac{\partial}{\partial z} \left(\rho_0 \frac{\overline{v'\theta'}}{(\partial\bar{\theta}/\partial z)} \frac{\partial\bar{\theta}}{\partial y} \right) + \frac{\partial}{\partial z} (\rho_0 \overline{w'\theta'}) \\ &= \frac{\partial}{\partial z} \left(\frac{\rho_0}{\langle \partial\bar{\theta}/\partial z \rangle + (\partial\bar{\theta}/\partial z)} \left[K_{yy} \left(\frac{\partial\bar{\theta}}{\partial y} \right)^2 \right. \right. \\ & \quad \left. \left. + K_{zz} \left(\left\langle \frac{\partial\bar{\theta}}{\partial z} \right\rangle + \frac{\partial\bar{\theta}}{\partial z} \right)^2 \right] \right), \end{aligned} \quad (37)$$

where the K s are the eddy diffusion tensor components. Thus, the overall thermal forcing becomes

$$\begin{aligned} J &= \frac{\bar{\theta} - \langle \bar{\theta} \rangle}{\tau_r} + \frac{1}{\rho_0} \frac{\partial}{\partial z} \left(\frac{\rho_0}{\langle \partial\bar{\theta}/\partial z \rangle + (\partial\bar{\theta}/\partial z)} \left[K_{yy} \left(\frac{\partial\bar{\theta}}{\partial y} \right)^2 \right. \right. \\ & \quad \left. \left. + K_{zz} \left(\left\langle \frac{\partial\bar{\theta}}{\partial z} \right\rangle + \frac{\partial\bar{\theta}}{\partial z} \right)^2 \right] \right). \end{aligned} \quad (38)$$

Now that the forcing terms have been parameterized, all that is needed to solve the dynamical equations are the seasonal temperature fields and estimates for the eddy diffusion coefficients and radiative time constants. The zonal winds are calculated using the thermal wind equation. The grid spacing must be set so

that there are no grid lines at or close to the equator, or at the poles, where the dynamical equations are not valid.

5. ADVECTIVE AND DIFFUSIVE TRANSPORT

In 1-D photochemical models, eddy and molecular diffusion are the only processes considered in the transport of molecular species. For 2-D photochemical models, advection becomes a major part of the tracer transport. On Earth, where orographic and planetary vorticity effects are prevalent, planetary waves are responsible for strong meridional tracer transport. The Earth's fast rotation is responsible for this planetary vorticity. On a slowly rotating body such as Titan, planetary vorticity effects are not expected. Therefore, advection is the dominant mode of meridional tracer transport and meridional diffusive transport can be neglected entirely.

Once the meridional velocity field is determined, the advection, Eq. (4), can be solved. This work uses the conservation of second-order moments advection algorithm developed by Prather (1986), modified for spherical coordinates. For each time step, the Prather method not only conserves the total tracer abundance (the zeroth-order moments) but also conserves the mean slope of the tracer distribution in each dimension (first-order moments) and the curvature in the tracer distribution, including cross terms (second-order moments). An advantage of the Prather method is that time steps can be used all the way up to the Courant limit. The Courant limit is reached when all the contents of a grid cell are transported in one time step. Additionally, the Prather method can maintain positive concentrations without introduction of numerical diffusion and can resolve tracer gradients on the order of the grid size. A detailed discussion of this method can be found in Shia *et al.* (1990).

Finally, the diffusion equation, Eq. (5), must be solved. In spherical coordinates this equation becomes

$$\frac{\partial n_i}{\partial t} = -\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \phi_i), \quad (39)$$

where

$$\phi_i = -(D_i + K_{zz}) \left[\frac{\partial n_i}{\partial r} + \frac{n_i}{T} \frac{\partial T}{\partial r} \right] - \left(\frac{D_i}{H_i} + \frac{K_{zz}}{H_0} \right) n_i. \quad (40)$$

In Eqs. (39) and (40), $n_i \equiv \mu_i N$ is the number density, H_i the scale height, and D_i the diffusion coefficient of the i th constituent. All other terms have previously been defined. Equation (39) is solved using a time-dependent, implicit, centered finite-difference algorithm.

Lower boundary conditions are treated in the same manner as in Yung *et al.* (1984). Upper boundary conditions are as follows. For short-lived chemical species, chemical equilibrium is assumed. For the remaining hydrocarbons, it is assumed that the diffusive flux through the upper boundary is balanced by the integrated net production of that species above the upper boundary. Only atomic and molecular hydrogen are assumed to undergo Jeans escape. For these two species, the diffusive flux through

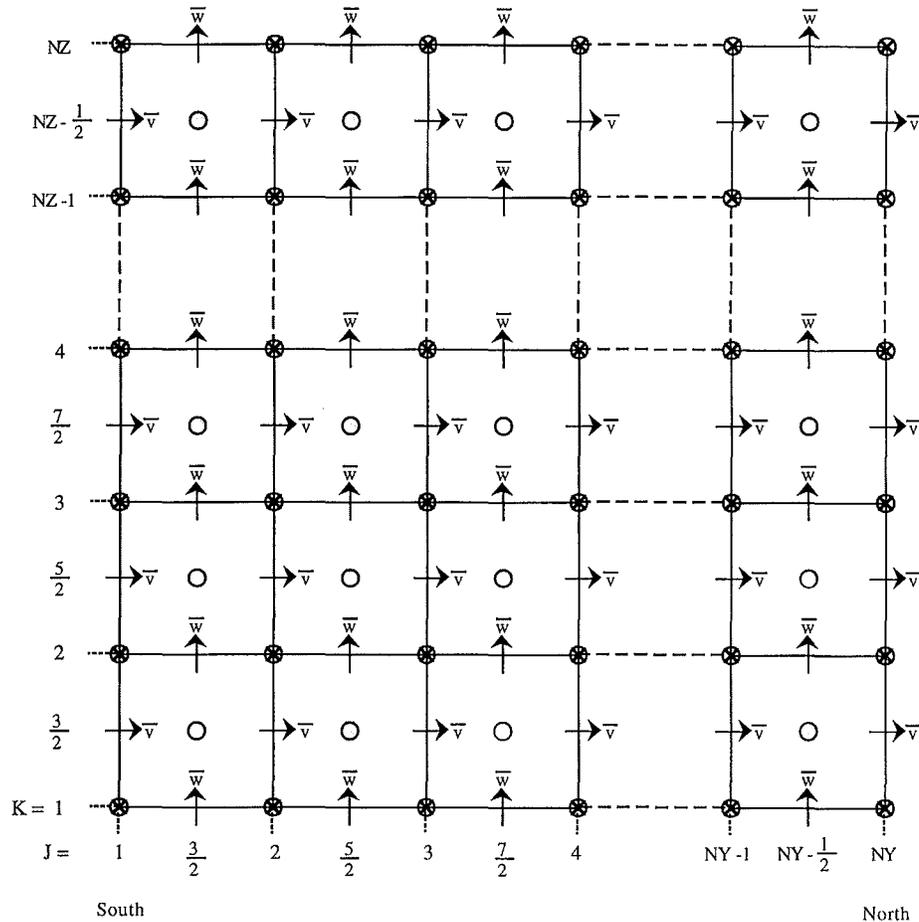


FIG. 1. Schematic representation of the grid used for the numerical model. There are $NY \times NZ$ grid points and $(NY-1) \times (NZ-1)$ cells. The number density is evaluated at the center of each cell (i.e., at $(J, K) = (3/2, 3/2)$, etc.). The vertical velocity component is calculated at the bottom of each cell ($(J, K) = (3/2, 1)$, etc.). The meridional velocity component is calculated at the left side of each cell ($(J, K) = (1, 3/2)$, etc.). The stream function is calculated at each grid point (J, K) . The curvature of the atmosphere is not shown in this representation.

the upper boundary is fixed by the integrated net production and the Jeans escape flux at the exobase.

6. THE TWO-DIMENSIONAL MODEL

The grid structure used for Titan's stratosphere is characterized in Fig. 1. In the meridional direction the grid points were restricted to the latitude range $(-85^\circ, +85^\circ)$. Latitude bins of 10° width were used, as they sufficiently resolved the meridional structure. The lower boundary, $z = 0$ in log pressure coordinates, is set at the tropopause, ≈ 40 km in real altitude. The upper boundary is set high in the stratosphere at 0.05 mbar pressure. The upper boundary is at 240 km in log pressure coordinates, corresponding to a real altitude of ~ 300 km. This upper boundary allows at least two scale heights above the altitudes where the weighting functions for the chemical species of interest peak (Coustenis *et al.* 1989, 1991, 1995). Equally important, this altitude range yields an atmospheric layer that is thin compared to the radius of the satellite, justifying the approximations made in the dynamical equations.

Because the density of the atmosphere decreases exponentially with altitude, the vertical resolution in the numerical model must be smaller than the scale height. A general rule of thumb for numerical resolution of an exponential is $\Delta z < H/3$. The minimum scale height in the region of interest occurs at the tropopause, where the minimum stratosphere temperature occurs. The scale height at the tropopause is approximately 15 km. Using $NZ = 60$ results in $\Delta z = 4.0$ km. This is sufficient to resolve the exponential pressure relationship and gives an 18×61 grid overall.

Radiative time constants, eddy diffusion coefficients, temperatures, and zonal wind velocities are required inputs for the model to perform chemical, dynamical, and diffusive transport calculations. Radiative time constants for Titan's atmosphere were estimated by Flasar *et al.* (1981). These are shown in Fig. 2a. A simple least-squares fit of this data is used in this model. The eddy diffusion coefficient is modeled after Strobel *et al.* (1992). Figure 2b shows the model eddy diffusion coefficients compared to those used in the 1-D photochemical models of Yung *et al.* (1984) and Toubanc *et al.* (1995).

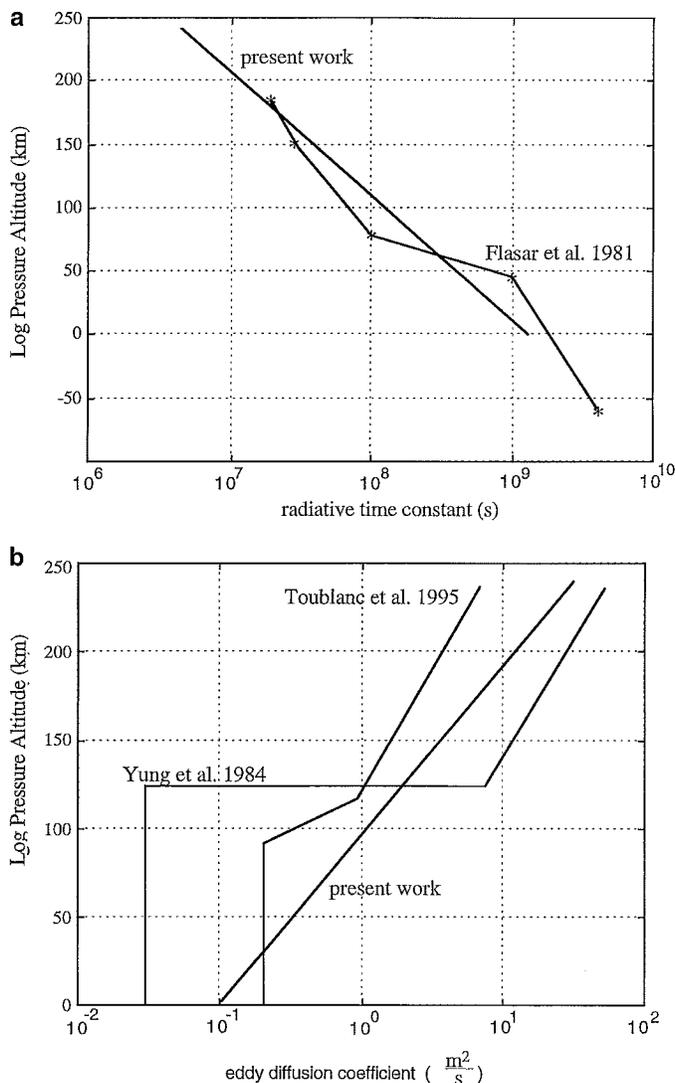


FIG. 2. (a) Radiative time constants for Titan's stratosphere. (b) Eddy diffusion coefficients for Titan's stratosphere. In log pressure coordinates $z=0$ corresponds to the tropopause.

Seasonal temperature profiles are modeled after Hourdin *et al.* (1995). They used an intensive radiative transfer model coupled with a GCM to generate solstice and equinox temperature fields. Their vertical temperature structure was modeled after Lellouch *et al.* (1989). Yelle (1991) showed a slight decrease in stratosphere temperatures above 1 mbar not incorporated into the model of Hourdin *et al.* In this work we empirically fit Hourdin *et al.*'s temperatures fields for Northern Hemisphere winter solstice and vernal equinox. We assume the temperature fields were reversed, symmetric around the equator for the summer solstice and autumnal equinox. Corrections were made for temperatures above 1 mbar to be consistent with the findings of Yelle (1991). Figure 3 shows the temperature profiles for equinox and solstice.

All numerical modeling to solve Eq. (1) is coded in FORTRAN 77 and run on a DEC 3000 VMS Workstation. The time step is 10^6 s, the maximum time step possible without exceed-

ing the Courant limit during numerical advection. A time step starts out by calculating the subsolar latitude. The subsolar latitude is then used as input to determine the temperature field and photolysis rates for each grid cell. Photolysis, chemical, and sublimation reactions are used to calculate the production and loss of each chemical species in each grid cell for the present time step. Molecular diffusion coefficients are determined from the temperature field. Diffusive and eddy transport calculations are then conducted. Finally, the velocity field is determined and advective transport calculations are performed.

Initial number densities for all latitudes are assigned by using the values calculated from the Yung *et al.* model. This assignment generally underestimates the abundance of hydrocarbons near the equator and overestimates their abundances near the poles. However, these initial guesses are found to always lead to convergence. The mixing ratio for CH_4 is held at 0.02 at the

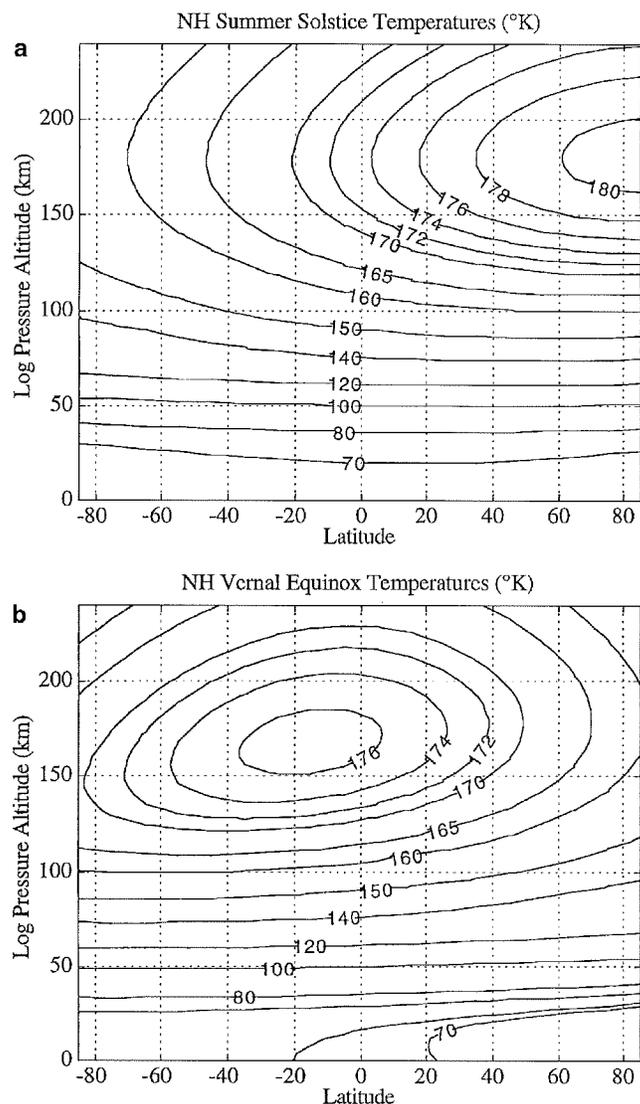


FIG. 3. Model temperature fields for (a) solstice and (b) equinox.

tropopause, resulting in the same mixing ratio throughout the stratosphere. Short-lived chemical species are not transported, saving valuable CPU time.

Since this is a time-dependent model, the number density of each species does not converge to a definite value in each grid cell. Instead, the number density of each species converges to a repeatable seasonal cycle. For a typical run of the code all species reach steady state in approximately 100,000 iterations (~ 107 equivalent Titan years) using approximately 100 h of CPU time.

7. MODEL RESULTS

Since CH_4 is well mixed in Titan's stratosphere, C_2H_6 is used to constrain the values for the forcing parameters. Figure 4a

shows the meridional distribution of C_2H_6 from the nominal model for northern vernal equinox. As seen in the figure, there is a marked equator-to-pole increase in C_2H_6 abundance in both hemispheres. To begin to understand the cause for the high latitude abundance enhancement, Fig. 4a should be compared to Fig. 4b. The data plotted in Fig. 4b are from a run of the code with the exact same conditions as those producing Fig. 4a, except that advection is turned off. Shutting off the advection essentially gives a one-dimensional photochemical model at each latitude, where the solar zenith angle and temperature field are allowed to vary with the seasons. In Fig. 4b the equator has the highest abundance of ethane, the opposite of what is seen in Fig. 4a. With no meridional transport, one would expect more ethane near the equator than near the poles, since more photolysis occurs annually near the equator than near the poles. It can be concluded that advective transport is responsible for differences seen between Figs. 4a and 4b. Physically, the average annual vertical velocities are positive at low latitudes (Hourdin *et al.*). The upward advective flux of ethane dominates the downward diffusive flux of ethane that is created high in the stratosphere. The result is that, instead of ethane produced near the equator being transported downward, it is advected horizontally where it collects at the poles. At the poles, the direction of the vertical velocity is upward for one season and downward for three seasons [Hourdin *et al.*], thus allowing downward diffusive transport to compete with vertical advective transport on an annual basis.

The meridional ethane profile from Voyager IRIS data is much more uniform between 53°S and 30°N latitudes than that seen in Fig. 4a (Coustenis and Bézard 1995). The ethane mixing ratios plotted in Fig. 4a were calculated with a strong meridional circulation. The mixing ratios plotted in Fig. 4b were calculated using no meridional circulation. A more uniform meridional ethane distribution can only be achieved in this two-dimensional photochemical transport model if a weaker meridional circulation is used in the advection calculations.

Coustenis and Bézard (1995) report altitude data for the contribution functions only for latitudes 53°S and 50°N . Therefore, this model will only attempt to reproduce the C_2H_6 mixing ratios for the grid points closest to those latitudes for the same season. It was determined that the radiative time constant had to be increased by a factor of 10 to weaken the meridional circulation sufficiently to reproduce those results. The decrease in the radiative time constant results in the dynamical turnover time being comparable to the photochemical lifetime of ethane. Figure 5 shows that the revised profile for vernal equinox has a much more meridionally uniform C_2H_6 abundance. For the time of the Voyager 1 encounter with Titan, Fig. 6 shows that the model C_2H_6 profiles are now in close agreement with the Voyager IRIS abundances.

Figures 7–9 show mixing ratio profiles for C_2H_2 , C_3H_8 , and CH_3CCH , respectively. These are the three most abundant hydrocarbon species in Titan's atmosphere after CH_4 and C_2H_6 . The Voyager data shown in these figures are the half-width levels for the contribution functions from Coustenis and Bézard. The results for these species all fall within the half-width altitudes.

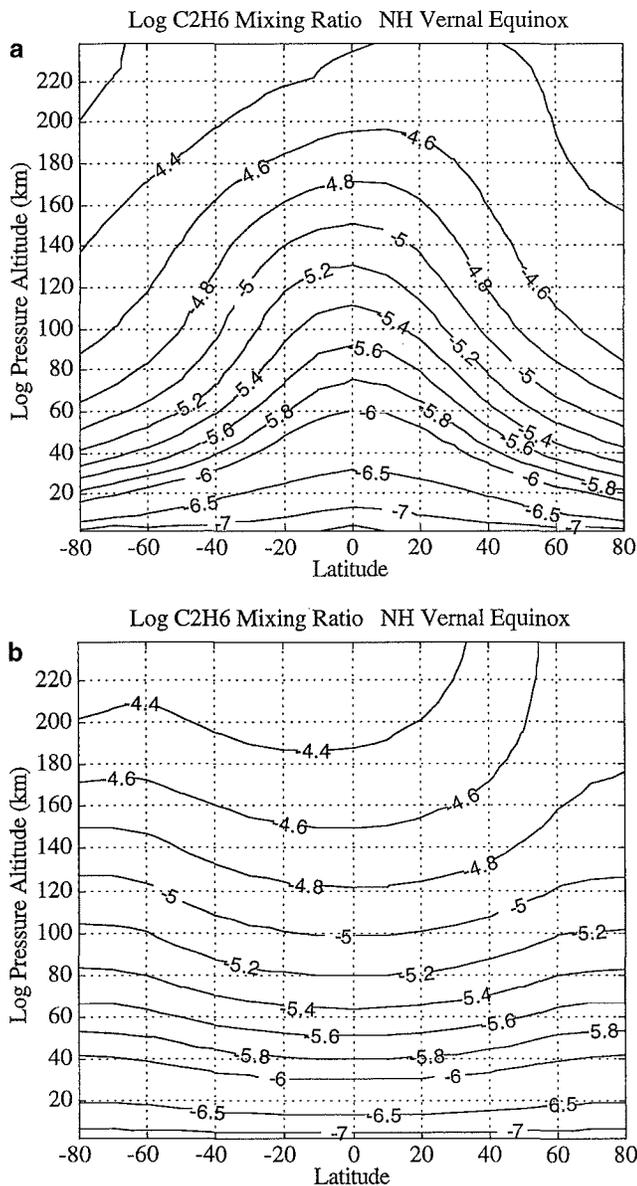


FIG. 4. Ethane abundances in Titan's stratosphere. (a) Full 2-D model with advection. (b) 2-D model with no advective transport.

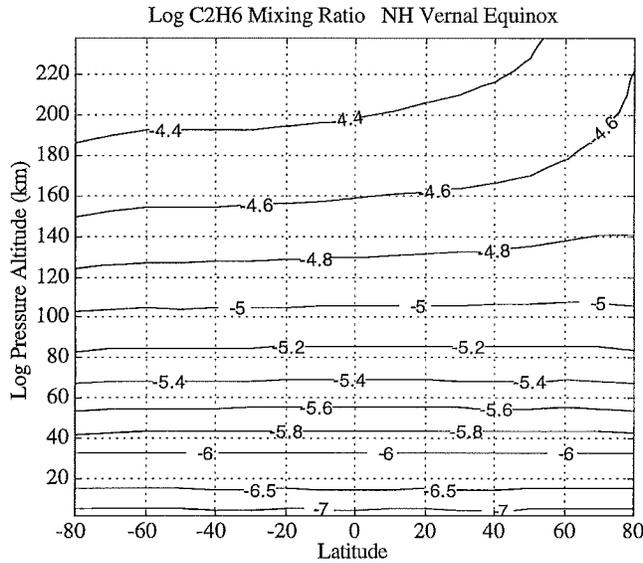


FIG. 5. Ethane abundances in Titan's stratosphere that result when the meridional circulation is weakened.

However, the model C_2H_2 mixing ratios are at the high mixing ratio extreme of the error bars, as was the case in previous 1-D models (Yung *et al.* 1984 and Lara *et al.* 1996).

Coustenis and Bézard also report an enrichment at $50^\circ N$ and $70^\circ N$ latitudes for some hydrocarbon species (C_2H_4 , C_3H_4 , and C_4H_2). Using their published altitudes for the maximum contribution functions for $53^\circ S$ and $50^\circ N$, Table VI has been generated to compare the model to the observational data. Table VI shows the composition ratios, $50^\circ N : 50^\circ S$, for these species, as well as those for C_2H_2 , C_3H_8 , and CH_3CCH . Recall that the strength of the meridional circulation was adjusted so that the C_2H_6 mixing

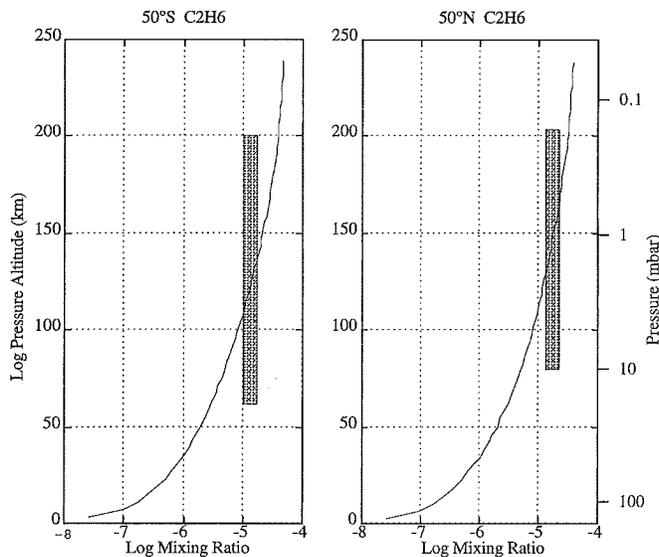


FIG. 6. Mixing ratio profiles for ethane at latitudes $50^\circ S$ and $50^\circ N$. For each latitude the model (curve) is compared to mixing ratios retrieved from Voyager IRIS data by Coustenis and Bézard (1995).

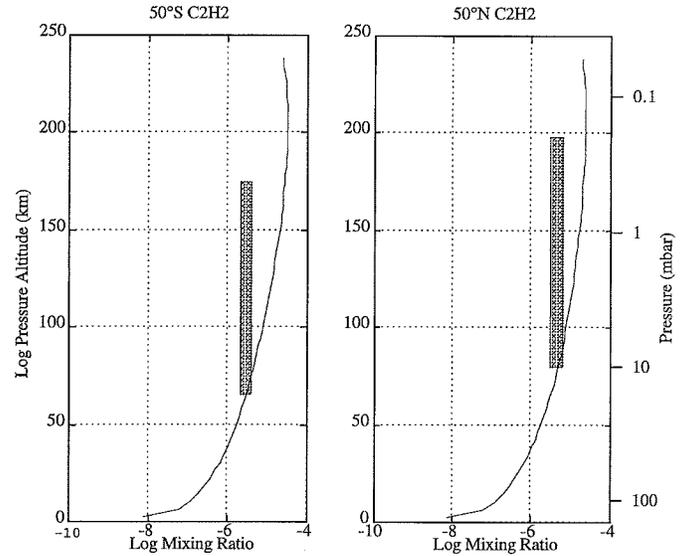


FIG. 7. Mixing ratio profiles for acetylene at latitudes $50^\circ S$ and $50^\circ N$. For each latitude the model (curve) is compared to mixing ratios retrieved from Voyager IRIS data by Coustenis and Bézard (1995).

ratios were in agreement with the observational data. This results in the model north-south abundance ratio for C_3H_8 being within the uncertainty from the observational data. The ratio for C_2H_2 is close to the calculated value, but as previously mentioned the model overestimates the amount of C_2H_2 (by factors of 3.8 and 2.6, respectively, for the two latitudes and altitudes in Table VI), resulting in a model ratio not exactly equal to the observed ratio.

No high-latitude enrichment is seen in the model for C_2H_4 . The model overestimates the C_2H_4 abundance at $50^\circ S$ by a factor of 3.5 and underestimates it by the same factor at $50^\circ N$. For C_3H_4

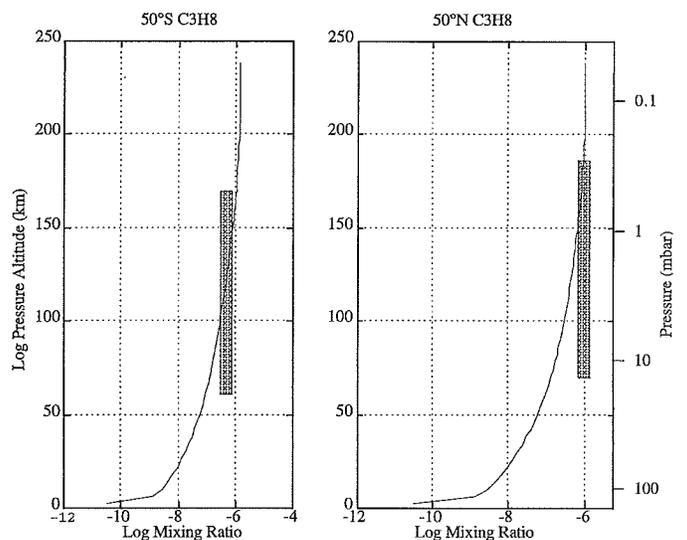


FIG. 8. Mixing ratio profiles for propane at latitudes $50^\circ S$ and $50^\circ N$. For each latitude the model (curve) is compared to mixing ratios retrieved from Voyager IRIS data by Coustenis and Bézard (1995).

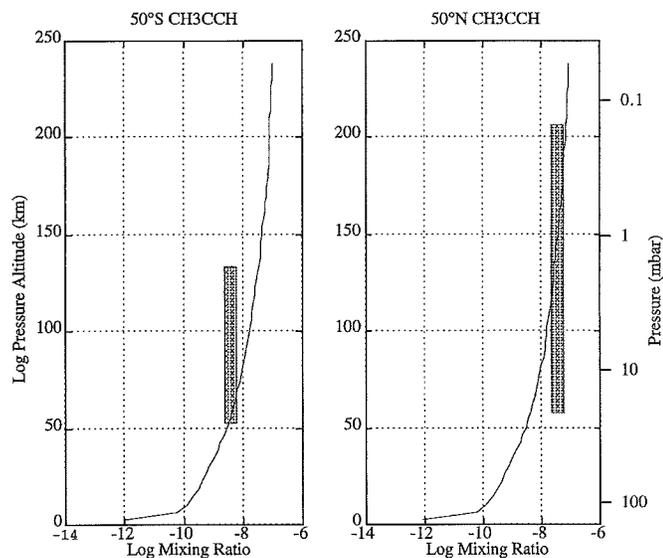


FIG. 9. Mixing ratio profiles for methylacetylene at latitudes 50°S and 50°N. For each latitude the model (curve) is compared to mixing ratios retrieved from Voyager IRIS data by Coustenis and Bézard (1995).

the model predicts a slight enrichment at 50°N over 50°S, but not an order of magnitude as observed. The smaller north-south ratio is entirely due to the model overestimating the CH₃CCH mixing ratio by a factor of 2.6 at 50°S. The model does its poorest in matching the abundances of C₄H₂. The model mixing ratio at both latitudes is overestimated by more than an order of magnitude. An enrichment is seen at 50°N over 50°S, but the north : south ratio is only 0.1 of that observed.

The seasonal variations in hydrocarbon abundances for a given latitude are shown in Fig. 10. Here, 50°N is chosen to be representative of mid-latitudes in both hemispheres. Column densities above 5 mbar are shown for C₂H₆, C₃H₈, C₂H₂, and CH₃CCH, showing how their abundances vary seasonally in the upper stratosphere. For these four species, the maximum column densities exceed the minimum values by 10, 14, 9.5, and 12%, respectively. The maximum column density for each occurs in mid-summer. This is because, although the maximum photolysis occurs at the solstice, the temperature field in the stratosphere lags behind the seasonal forcing. The maximum stratosphere

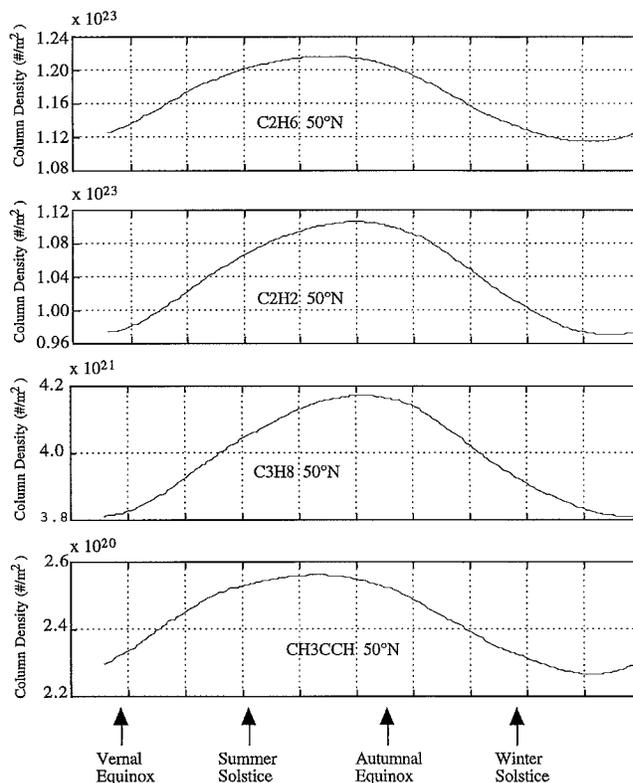


FIG. 10. Column densities above 5 mbar for C₂H₆, C₂H₂, C₃H₈, and CH₃CCH at 50°N latitude as a function of season.

temperatures occur in late summer. The peak column densities occur between the times of peak photolysis and the peak temperature, when temperature-dependent chemical reaction rates are maximum. Seasonal variations for latitudes above 50° are slightly greater than those shown in Fig. 10 while very small seasonal variations for these hydrocarbons are predicted by the model for the equator.

All chemical species more massive than C₄H₃ in this model are lumped together and called polymers. Once produced, the polymers will be photolyzed, condense, or participate in reactions to produce larger molecules. Most of the polymers are photodissociated back into smaller hydrocarbons. However, some long-chain hydrocarbons are produced and are irreversibly removed, creating the aerosol layers present in Titan's stratosphere. Heavy hydrocarbon compounds were not tracked in this photochemical model. Although the photochemical loss and condensation rates for the polymers are not calculated in this model, an upper limit for their production rate is approximated by the sum of the reaction rates of the polymer-producing reactions.

Figure 11 displays the seasonal column production rates for polymers for latitudes 0°, 20°N, 50°N, and 80°N. The production rate profiles for southern hemisphere latitudes would be analogous to the northern hemisphere latitudes displayed in this figure. In Fig. 11, the column production rates for equatorial latitudes (0°–20°) are fairly constant throughout the year. At 50°N,

TABLE VI
Hemispheric Gas Composition Comparison

| Molecule | 50°S mixing ratios | 50°N mixing ratios | North/south model | North/south observed ^a |
|-------------------------------|-----------------------|-----------------------|----------------------|--------------------------------------|
| C ₂ H ₂ | 1.05×10^{-5} | 1.46×10^{-5} | 1.4 | 2.2 ± 0.5 |
| C ₂ H ₄ | 5.28×10^{-7} | 2.86×10^{-7} | 0.5 | 7 ± 3 |
| C ₂ H ₆ | 1.33×10^{-5} | 2.39×10^{-5} | 1.8 | 1.6 ± 0.2 |
| CH ₃ CCH | 1.88×10^{-9} | 2.85×10^{-9} | 1.5 | 9.5 ± 2 |
| C ₃ H ₈ | 2.11×10^{-7} | 4.17×10^{-7} | 2.0 | 1.7 ± 0.7 |
| C ₄ H ₂ | 1.81×10^{-7} | 4.71×10^{-7} | 2.6 | 23 ± 4 |

^a From Table III, Coustenis and Bézard (1995).

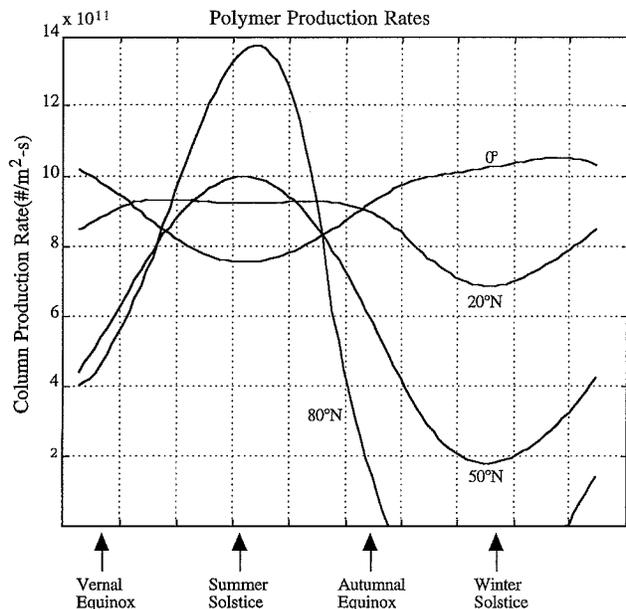


FIG. 11. Column production rates of polymers in Titan's stratosphere as a function of season.

the production rate in the summer peaks at a value 5 times greater than the minimum production rate in the winter. The extrema in production rates occur at polar latitudes, where the production rate in the summer is 25% greater than the production rate at 50°N and 40% greater than at the equator. During the polar winter, the production of polymers ceases altogether as the supply of free radicals ends due to the absence of sunlight.

8. DISCUSSION

The coupling of dynamics, thereby advection, photochemistry, and diffusion in two-dimensional photochemical models makes it difficult to determine which parameters need adjustment to accurately match observational data. Changes in any dynamical parameter, chemical reaction rate, or boundary condition can notably change the overall seasonal distribution of most of the chemical species. This work attempted to simplify the problem by limiting the vertical extent of the region of interest, the number of chemical species, and the number of chemical reactions.

The vertical region of interest, from the tropopause to 0.05 mbar, may appear to be well below where most of the CH₄ photolysis occurs. However, this region of Titan's atmosphere is dominated by photosensitized destruction of CH₄ (Yung *et al.* 1984). The photosensitized destruction of CH₄ is brought about by the photolysis of C₂H₂ and C₄H₂, both of which are as readily photolyzed in this region as they are higher in the atmosphere. Therefore, the model mole fractions of C₂H₆ and C₃H₈, the two most abundant hydrocarbons after CH₄ and the two major products of CH₄ destruction, produced in this region of the atmosphere should be accurate. When the strength of the model meridional circulation is adjusted to match the observed ethane

abundances for 50°S and 50°N latitudes, the results for both C₂H₆ and C₃H₈ are quite satisfactory.

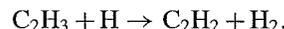
For CH₃CCH, the model is fairly accurate in matching the observed abundances at 50°N; however, as previously mentioned, the model abundance is high at 50°S, resulting in a smaller north-south ratio than what was observed. However, the model comes closer to the observed abundances than previous 1-D models (Yung *et al.* 1984, Toublane *et al.* 1995, and Lara *et al.* 1996).

A serious shortcoming of the model is the failure to more closely match C₂H₂ with the Voyager data. Model values for 50°S and 50°N are high by factors of 3.8 and 2.6, respectively. Model abundances for C₄H₂ are high by even larger factors, since the production of C₄H₂ is strongly coupled to the C₂H₂ abundance. Our model abundances for C₂H₄ also fail to closely match the Voyager data. The model abundance is a factor of 3.5 high at 50°S, and it is low by the same factor at 50°N. Toublane *et al.* (1995) had a more difficult time matching the Voyager C₂H₄ abundance; however, Lara *et al.* (1996) had quite good results.

In limiting the number of chemical reactions, the model did not incorporate the reaction



neglecting it in favor of the faster reaction



After this work was completed we became aware of calculations by Monke *et al.* (1995) showing that the above three-body reaction is much faster than previously thought. This reaction may now be important for the catalytic conversion of C₂H₂ into C₂H₆ in Titan's stratosphere. The absence of this reaction in the model may explain the high C₂H₂ and C₄H₂ mixing ratios.

As noted for all but one of the species in Table VI, both the Voyager data and the model show higher mixing ratios at 50°N than at 50°S. From our model we conclude that this may be an altitude effect in addition to a latitude effect. As the previously cited 1-D photochemical models have demonstrated, the mixing ratios for these hydrocarbon species increase with altitude. The contribution functions for the Voyager data for these species have maxima at higher altitudes for 50°N than for 50°S. We encourage the publication of the weighing function altitudes for the other latitudes so that we may determine to what extent the hydrocarbon enrichment at even higher northern latitudes is due to a real meridional enrichment and to what extent it is an altitude effect.

Some of the physical parameters incorporated into this work (e.g., K_{zz} , τ_r , and effect of aerosols on attenuating the solar flux) were taken from 1-D studies of Titan's atmosphere and relied on data that was either globally averaged or taken from limited latitude regions. One-dimensional models assume these parameters are a function of altitude only, but in reality these parameters are also functions of latitude and time (season). To keep the present

model simple, no attempt was made to determine meridional and seasonal variations in these parameters. Such an undertaking would be very difficult, if possible at all, with our limited knowledge of Titan's atmosphere.

Although this model limited the vertical extent of the atmospheric region of interest, the diffusive flux of molecular species through the upper boundary did incorporate meridional and season effects though the choice of the upper boundary conditions for the long-lived chemical species. These boundary conditions depend strongly on the temperature and photolysis rates at the upper boundary. The temperatures at the upper boundary are representative of the temperatures well above the boundary; however, the photodestruction rates of several of the chemical species (most importantly C_2H_6 and C_2H_4) are greater above the upper boundary than at the boundary. This likely introduces incorrect diffusive fluxes at the upper boundary and contributes to the shortcomings of the model.

This model was a first attempt at a simple 2-D photochemical transport model for Titan's stratosphere. Further modeling should be attempted which incorporates the coupling of photochemistry with radiative transfer and seasonal aerosol production models. Such coupling will result in more reliable seasonal temperature fields and photolysis rates. They should also be coupled with dynamical models that are accurate for a much greater vertical extent.

The Cassini mission is expected to monitor Titan between 2004 and 2008. This should add a wealth of new data on the seasonal variations in Titan's atmosphere as this mission will take place during early northern hemisphere winter, one season earlier than the Voyager encounters. Detailed meridional temperature data will allow for more accurate photochemical and dynamical modeling. In addition, close-up observations of atmospheric features should greatly improve our knowledge of zonal wind velocities which are needed in order to accurately determine meridional velocity fields for transport calculations.

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